

# 14.581 International Macroeconomics

## — Lecture 17: Fragmentation (Theory) —

# Today's Plan

- ① Trade in Tasks
- ② Sequential Production
- ③ Multinational Production

# Fragmentation of production

Do we really need new theories?

- In the previous lecture, we have discussed how to measure fragmentation using global input-output tables
- **Question:**  
Is “fragmentation” just a fancy name for “trade in intermediate goods”? Can we just relabel final goods as intermediates and recycle existing trade models?
- **Some answer(s):**
  - ① It is about trade in intermediate goods, but new models emphasize differences in trade costs across goods (e.g. how routine a particular “task” may be), which previous models abstract from
  - ② Sequential nature of production may also introduce new considerations (e.g. the magnification of trade costs that we saw in Yi 2003 and Yi 2010)
  - ③ It is *not just* about trade in intermediate goods, since “fragmentation” also usually includes a transfer of technology from one country to another (since same firm may be active in multiple countries)
- In the rest of this class we'll discuss a number of neoclassical models aimed to shed light on these new considerations

# 1. Trade in Tasks

# Grossman and Rossi-Hansberg (2008)

## Assumptions

- As in Heckscher-Ohlin model:
  - There are two countries, Home and Foreign
  - There are 2 tradeable goods,  $i = 1, 2$
  - There are two factors of production,  $L$  and  $H$
- In contrast with Heckscher-Ohlin model:
  - Production process involves a large number of *tasks*  $j \in [0, 1]$
- Tasks are of two types:
  - $L$ -tasks which require 1 units of low-skilled labor
  - $H$ -tasks which require 1 units high-skilled labor

# Grossman and Rossi-Hansberg (2008)

## Offshoring Costs

- Tasks vary in their offshoring costs
  - because some tasks are easier to codify
  - because some services must be delivered personally, while others can be performed at a distance with little loss in quality
- To capture this idea, GRH assume that:
  - $H$ -tasks cannot be offshored
  - $L$ -tasks can be offshored, but amount of low-skilled labor necessary to perform task  $j$  abroad is given by  $\beta t(j) > 1$
- Under this assumption,
  - $\beta$  reflects overall feasibility of offshoring at a point in time (e.g. communication technology)
  - $t(j)$  is an increasing function which captures differences in offshoring costs across tasks (e.g. cleaning room vs. call center)

# Grossman and Rossi-Hansberg (2008)

## The Offshoring Decision

- Suppose that wages for low-skilled labor are higher at Home

$$w_L > w_L^*$$

- Benefit of offshoring  $\equiv$  lower wages abroad
- Cost of offshoring  $\equiv$  loss in productivity captured by  $\beta t(j)$
- In a competitive equilibrium, firm will offshore tasks if and only if:

$$\beta t(j) w_L^* < w_L$$

- Let  $J \in [0, 1]$  denote the marginal task that is being offshored

$$\beta t(J) w_L^* = w_L \tag{1}$$

# Grossman and Rossi-Hansberg (2008)

## Offshoring as Factor Augmenting Technological Change

- The cost of producing one unit of some good is given by

$$c_i = a_{Li} [w_L(1 - J) + w_L^* \beta T(J)] + a_{Hi} w_H \quad (2)$$

with  $T(J) \equiv \int_0^J t(j) dj$ ,  $w_H \equiv$  wage of high-skilled workers at Home

- Substituting (1) into (2), we obtain

$$c_i = a_{Li} w_L \Omega + a_{Hi} w_H$$

where  $\Omega = (1 - J) + \frac{T(J)}{t(J)} < 1$

- This looks just like the cost equation of a firm that employs low-skilled workers whose productivity is (inversely) measured by  $\Omega$ 
  - Hence, offshoring is economically equivalent to labor-augmenting technological progress



# Grossman and Rossi-Hansberg (2008)

## Productivity effect

- **Proposition** *If Home is a small open economy that produces both goods, a decrease in  $\beta$  increases  $w_L$*

- **Proof:**

- 1 Zero profit requires:

$$p_i = a_{Li}w_L\Omega + a_{Hi}w_H, \quad i = 1, 2$$

- 2 Since Home a small open economy,  $p_i$  does not depend on  $\beta$
- 3 This implies that  $w_L\Omega$  (and  $w_H$ ) do not depend on  $\beta$  either
- 4 Since  $\Omega$  is decreasing in  $\beta$ , we get  $w_L$  increasing in  $\beta$

# Grossman and Rossi-Hansberg (2008)

## Other effects

- **Productivity effect** implies that workers whose jobs are being offshored benefit from decrease in offshoring costs
- In general, a decrease in offshoring costs would also have:
  - ① **Relative-price effect.** If country is not small compared to the rest of the world, changes in  $\beta$  will also affect  $p_2/p_1$
  - ② **Labor-supply effect.** If there are more factors than produced goods, changes in  $\beta$  will also affect  $w_L\Omega$  and  $w_H$  at constant prices
- Simplest way to illustrate labor-supply effect is to consider case where Home is completely specialized in one good
  - this is the effect that has received the most attention in popular discussions
  - empirically, is it more or less important than the other two?

## 2. Sequential Production

# An Example of Sequential Production

Global Semiconductor Industry



# An Example of Sequential Production

Global Semiconductor Industry



# An Example of Sequential Production

Global Semiconductor Industry



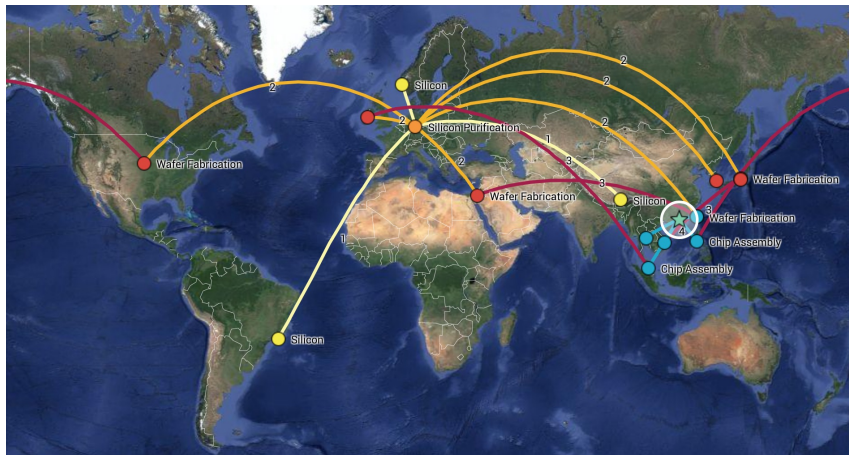
# An Example of Sequential Production

## Global Semiconductor Industry



# An Example of Sequential Production

## Global Semiconductor Industry





# Costinot, Vogel, and Wang (2013)

An elementary theory of global supply chains

- A simple trade model with sequential production:
  - Multiple countries, one factor of production (labor), and one final good
  - Production of final good requires a continuum of intermediate stages
  - Each stage uses labor and intermediate good from previous stage
  - Production is subject to mistakes (Sobel 1992, Kremer 1993)
- Key simplifications:
  - Intermediate goods only differ in the order in which they are performed
  - Countries only differ in terms of failure rate
  - All goods are freely traded

# Costinot, Vogel, and Wang (2013)

## Basic Environment

- Consider a world economy with multiple countries  $c \in \mathcal{C} \equiv \{1, \dots, C\}$
- There is one factor of production, labor:
  - Labor is inelastically supplied and immobile across countries
  - $L_c$  and  $w_c$  denote the endowment of labor and wage in country  $c$
- There is one final good:
  - To produce the final good, a continuum of stages  $s \in \mathcal{S} \equiv (0, S]$  must be performed (more on that on the next slide)
- All markets are perfectly competitive and all goods are freely traded
  - We use the final good as our numeraire

# Costinot, Vogel, and Wang (2013)

## Basic Environment (Cont.)

- At each stage, producing 1 unit of intermediate good requires a fixed amount of previous intermediate good and a fixed amount of labor
  - “Intermediate good 0” is in infinite supply and has zero price
  - “Intermediate good  $S$ ” corresponds to final good mentioned before
- Mistakes occur at a constant Poisson rate,  $\lambda_c > 0$ 
  - $\lambda_c$  measures total factor productivity (TFP) at each stage
  - Countries are ordered such that  $\lambda_c$  is strictly decreasing in  $c$
- When a mistake occurs, intermediate good is entirely lost
- Formally, if a firm combines  $q(s)$  units of intermediate good  $s$  with  $q(s)ds$  units of labor, the output of intermediate good  $s + ds$  is

$$q(s + ds) = (1 - \lambda_c ds) q(s)$$

# Costinot, Vogel, and Wang (2013)

## Free trade equilibrium

- In spite of arbitrary number of countries, unique free trade equilibrium is characterized by simple system of first-order difference equations
- This system can be solved recursively by:
  - 1 Determining assignment of countries to stages of production
  - 2 Computing prices sustaining that allocation as an equilibrium outcome
- Free trade equilibrium always exhibits vertical specialization:
  - 1 More productive countries, which are less likely to make mistakes, specialize in later stages of production, where mistakes are more costly
  - 2 Because of sequential production, *absolute productivity differences* are a source of *comparative advantage* between nations
- Cross-sectional predictions are consistent with:
  - 1 “Linder” stylized facts
  - 2 Variations in value added to gross exports ratio (Johnson Noguera 12)

- Comprehensive exploration of how technological change, either *global* or *local*, affects different participants of a global supply chain
- Among other things, we show that:
  - ① Standardization—uniform decrease in failure rates around the world—can cause welfare loss in rich countries: a strong form of immiserizing growth
  - ② Spillover effects are different at the bottom and the top of the chain: monotonic effects at the bottom, but not at the top
- **Broad message:** *Important to model sequential nature of production to understand consequences of technological change in developing and developed countries on trading partners worldwide*

# Antràs and de Gortari (2017)

## Adding General Geography of Trade Costs

- Consider optimal location of production for the different stages in a sequential GVC
- Without trade frictions  $\approx$  standard multi-country sourcing model
- With trade frictions, matters become trickier
- Location of a stage takes into account upstream and downstream locations
  - Where is the good coming from? Where is it going to?
  - Need to solve jointly for the optimal path of production

# Antràs and de Gortari (2017)

## A Multi-Stage Ricardian Model

- Framework will accommodate:
  - Ricardian differences in technology across stages and countries
  - A continuum of final goods
  - Multiple GVCs producing each of these final goods
  - An arbitrary number of countries  $J$  and stages  $N$
- Model will **not** predict the path of each specific GVC. Instead:
  - Characterize the relative prevalence of different possible GVC
  - Study average positioning of countries in GVCs
    - Intuitively, countries facing higher trading frictions should tend operate more upstream, where gross output losses associated with those tend to be lower
    - Related to Sobel/Kremer/CVW's channel
  - Trace implications for the world distribution of income

- Preferences are

$$u\left(\left\{y_i^N(z)\right\}_{z=0}^1\right)=\left(\int_0^1\left(y_i^N(z)\right)^{(\sigma-1) / \sigma} d z\right)^{\sigma /(\sigma-1)}, \quad \sigma>1$$

- Technology features CRS and Ricardian technological differences

$$p_j^F(\ell)=\tau_{\ell(N) j} \times \prod_{n=1}^{N-1}\left(\tau_{\ell(n) \ell(n+1)}\right)^{\beta_n} \times \prod_{n=1}^N\left(a_{\ell(n)}^n c_{\ell(n)}\right)^{\alpha_n \beta_n}$$

with  $\alpha_n$  = share of composite input at stage  $n$  and  $\beta_n=\prod_{m=n+1}^N\left(1-\alpha_m\right)$

- Composite input = labor and CES aggregator in  $u(\cdot)$

- $c_i=\left(w_i\right)^{\gamma_i}\left(P_i\right)^{1-\gamma_i}$ , where  $P_i$  is the ideal consumer price index



- In Eaton and Kortum (2002) with  $N = 1$ , they assume  $1/a^j(z)$  is drawn for each good  $z$  independently from the Fréchet distribution

$$\Pr(a_n^j(z) \geq a) = e^{-T_j a^\theta}, \text{ with } T_j > 0$$

- **Problem:** The distribution of the product of Fréchet random variables is **not** distributed Fréchet
  - The same would be true with fixed proportions (sum of Fréchets)
- How can one recover EK's magic in a multi-stage setting?

# Antràs and de Gortari (2017)

## The Challenge: Two Solutions

- ① If a production chain follows the path  $\{\ell(1), \ell(2), \dots, \ell(N)\}$ , then

$$\Pr \left( \prod_{n=1}^N \left( a_{\ell(j(n))}^n \right)^{\alpha_n \beta_n} \geq a \right) = \exp \left\{ -a^\theta \prod_{n=1}^N \left( T_{\ell(n)} \right)^{\alpha_n \beta_n} \right\}$$

- Randomness can be interpreted as uncertainty on compatibility
- ② Decentralized equilibrium in which stage-specific producers do not observe realized prices before committing to sourcing decisions
- Firms observe the productivity levels of their potential direct (or tier-one) suppliers
  - But not of their tier-two, tier-three, etc. suppliers

- Likelihood of a particular GVC ending in  $j$  is

$$\pi_{\ell j} = \frac{\left(\tau_{\ell j(N)j}\right)^{-\theta} \times \prod_{n=1}^{N-1} \left(\tau_{\ell j(n)\ell j(n+1)}\right)^{-\theta\beta_n} \times \prod_{n=1}^N \left(\left(c_{\ell j(n)}\right)^{-\theta} T_{\ell j(n)}\right)^{\alpha_n\beta_n}}{\Theta_j}$$

where  $\Theta_j$  is the sum of the numerator over all possible paths

- Notice that trade costs again matter more downstream than upstream
- Can compute final-good trade shares and intermediate input shares as explicit functions of  $T_j$ 's,  $c_j$ 's, and  $\tau_{ij}$ 's (conditional probabilities)
- Can also express labor market clearing as a function of transformations of these probabilities

# Antràs and de Gortari (2017)

## Gains from Trade

- Consider a 'purely-domestic' value chain that performs all stages in a given country  $j$  to serve consumers in the same country  $j$
- Such value chain captures a share of country  $j$ 's spending equal to

$$\pi_{jN} = \Pr(j, j, \dots, j) = \frac{(\tau_{jj})^{-\theta(1+\sum_{n=1}^{N-1} \beta_n)} \times (c_j)^{-\theta} T_j}{\Theta_j}$$

- We can then show

$$\frac{w_j}{P_j} = \left( \kappa (\tau_{jj})^{1+\sum_{n=1}^{N-1} \beta_n} \right)^{-1/\gamma_j} \left( \frac{T_j}{\pi_{jN}} \right)^{1/(\theta\gamma_j)}$$

- Under autarky  $\pi_{jN} = 1$ , so the (percentage) real income gains from trade, relative to autarky, are given by

$$\left( \pi_{jN} \right)^{-1/(\theta\gamma_j)} - 1$$

# Antràs and de Gortari (2017)

## Calibration to World-Input Output Database

- Map multi-country Ricardian framework to world Input-Output Tables
- World Input Output Database: Released in 2016
- 43 countries (86% of world GDP) + ROW
- Yearly: 2000-2014 (use 2014 data)
- Provides information on input and final output flows across countries

		Input use & value added			Final use			Total use
		Country 1	...	Country $J$	Country 1	...	Country $J$	
Intermediate inputs supplied	Country 1							
	...							
	Country $J$							
Value added								
Gross output								

- Normalizing  $\tau_{ii} = 1$ , it turns out that

$$(\tau_{ij})^{-\theta} = \sqrt{\frac{\pi_{ij}^F \pi_{ji}^F}{\pi_{ii}^F \pi_{jj}^F}}$$

- Estimate  $(T_j, \gamma_j)$  for all  $j$  and  $\alpha_n$  for all  $n$  targeting:
  - Diagonal of intermediate input and final-good share matrices
  - Ratio of value added to gross output by country
  - GDP shares by country (also take into account trade deficits)

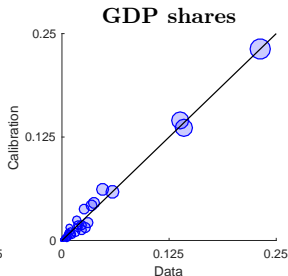
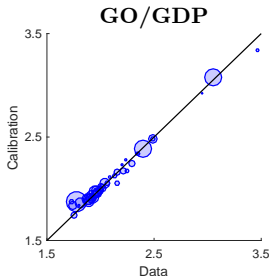
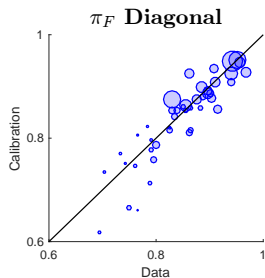
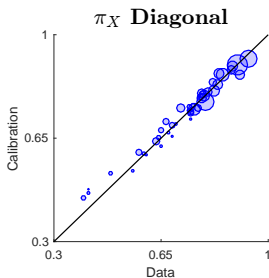
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- Estimate  $(T_j, \gamma_j)$  for all  $j$  and  $\alpha_n$  for all  $n$  targeting:
  - Diagonal of intermediate input and final-good share matrices
  - Ratio of value added to gross output by country
  - GDP shares by country (also take into account trade deficits)
- We set  $N = 2$  (so far data is 'rejecting'  $N > 2$ ) and  $\theta = 5$
- We find  $\alpha_2 = 0.16$  (remember  $\alpha_1 = 1$  by assumption)
  - Hence, data rejects a standard roundabout model ( $\alpha_2 = 1$ )

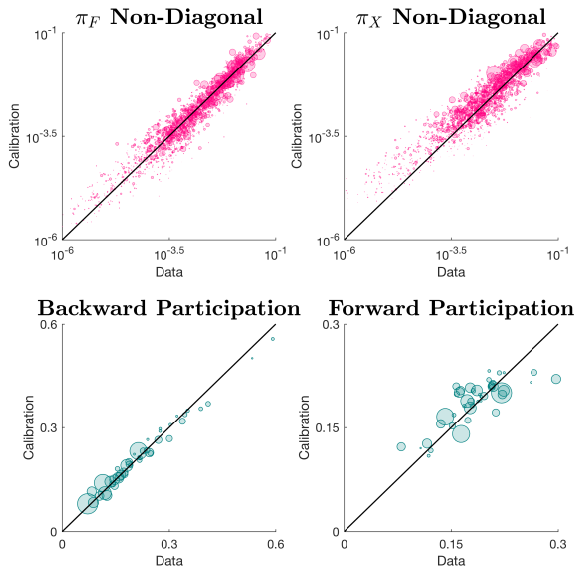
# Antràs and de Gortari (2017)

## Fit of the Model: Targeted Moments



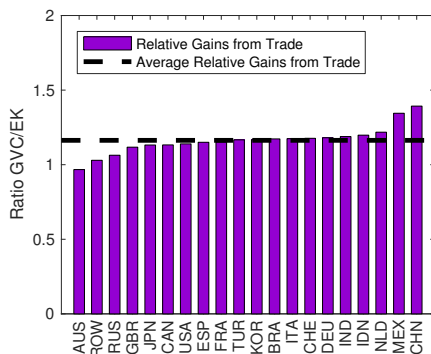
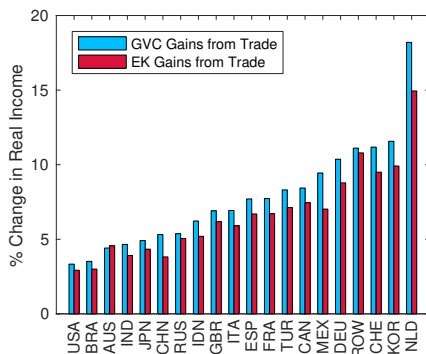


# Fit of the Model: Untargeted Moments



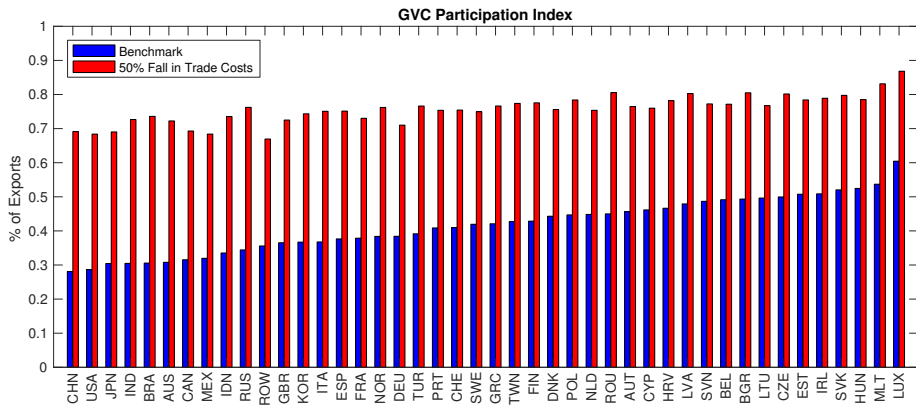
# Antràs and de Gortari (2017)

## Counterfactuals: Real Income Gains Relative to Autarky



- GVC model with  $N = 1$ , i.e. EK model, underestimates gains from trade by 17.5% on average

- All countries integrate more

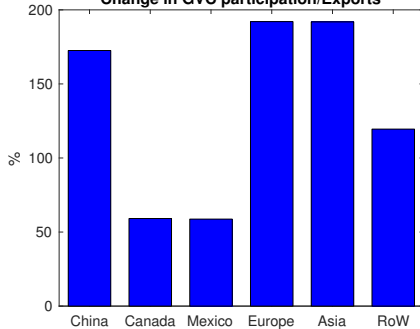


# Antràs and de Gortari (2017)

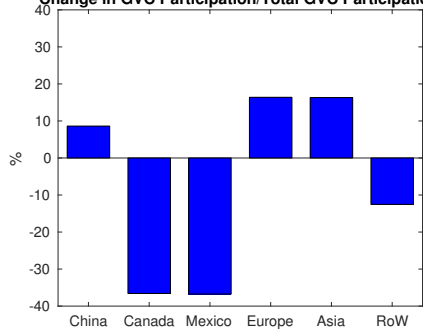
Counterfactuals: 50% Fall in Trade Costs

- USA integrates more with all regions...
- ...but global integration increases relative to regional integration

**Change in GVC participation/Exports**



**Change in GVC Participation/Total GVC Participation**



### 3. Multinational Production

# Ramondo and Rodriguez-Clare (2013)

## Basic Model

- Extension of Eaton and Kortum (2002) with both trade and multinational production (MP)
- For each good  $v \in (0, 1)$ :
  - Ideas gets originated in country  $i = 1, \dots, I$
  - Production takes place in country  $l = 1, \dots, I$
  - Consumption takes place in country  $n = 1, \dots, I$
- Trade versus MP:
  - If  $l \neq n$ , then good  $v$  is traded
  - If  $i \neq l$ , then MP occurs (in EK,  $i = l$ )

# Ramondo and Rodriguez-Clare (2013)

## Basic Model (Cont.)

- Model is Ricardian:
  - Labor is the only factor of production
  - Constant returns to scale
  - (Like EK, full model also includes tradable intermediate goods)
- Constant unit cost of production *and* delivery for a good  $v$  given by

$$\frac{d_{nl} h_{li} c_{li}}{z_{li}(v)}$$

where:

- $d_{nl} \equiv$  iceberg trade costs from country  $l$  to country  $n$
- $h_{li} \equiv$  iceberg costs from using technology from  $i$  in  $l$
- $c_{li} \equiv$  average unit cost of production for firms from  $i$  in country  $l$
- $z_{li}(v) \equiv$  productivity of firms from  $i$  producing good  $v$  in country  $l$
- $\mathbf{z}_i(v) \equiv (z_{1i}(v), \dots, z_{li}(v))$  is drawn from multivariate Fréchet

- **Main result:**

- Gains from trade are larger in the presence of MP because trade facilitates MP
- Gains from openness are larger than gains from trade because of MP and complementarity between trade and MP

- A model of MP without a model of MNEs?:

- in any given country and sector, technology is assumed to be freely available to a large number of price-taking firms
- discipline only comes from aggregate predictions of the model



- **North-North Fragmentation:**

- In GRH (2008), rationale for offshoring  $\equiv$  factor price differences
- More important for “North-South,” but not “North-North” fragmentation
- In GRH (2012), rationale for offshoring  $\equiv$  EES (at the task level)

- **Open Questions:**

- Can static models really get at sequential nature of GVCs?
  - Kim and Shin (AER, 2012) study payment delays as a way to provide incentives along a supply chain. Interesting connection between GVCs and trade finance
- How do GVCs affect gains from trade, incentives for trade protection, industrial policy etc.?
  - Blanchard, Bown and Johnson (2016) offer an interesting first attempt. Much more needed