

Econ 266 International Trade  
— Lecture 1 —  
Comparative Advantage and Gains from Trade

# Today's Plan

- 1 Course logistics
- 2 A Brief History of the Field
- 3 Neoclassical Trade: Standard Assumptions
- 4 Neoclassical Trade: General Results
  - 1 Gains from Trade
  - 2 Law of Comparative Advantage

- **Lecture:** Monday and Wednesday 11:30AM-1:20PM
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  - Office hours: just email me

- No required textbooks, but you will frequently find it helpful to refer to:
  - Dixit and Norman, *Theory of International Trade*
  - Feenstra, *Advanced International Trade: Theory and Evidence*

- **Course requirements:**

- 15 short 'paper responses' (roughly one per week): 50% of the course grade
- One mock referee report: 20% of the course grade
- One research proposal: 30% of the course grade

- **Course outline:**

- ① General setup (gains from trade, comparative advantage) [2 lectures]
- ② Ricardian and Assignment Models [5 lectures]
- ③ “New” trade theory (trade with increasing returns to scale) [2 lectures]
- ④ Firm-level Trade [4 lectures]
- ⑤ Gravity Models [3 lectures]
- ⑥ Economic Geography [3 lectures]

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# A Brief History of the Field

Two hundred years of theory

## ① 1830-1980: Neoclassical trade theory

⇒ Ricardo

⇒ Heckscher-Ohlin-Samuelson

⇒ Dixit-Norman

## ② 1980-1990: “New” trade theory

⇒ Krugman-Helpman

⇒ Brander-Krugman

⇒ Grossman-Helpman

# A Brief History of the Field

The discovery of trade data

- 1 **1990-2000: Empirical trade**
- 2 **2000-2010: Firm-level heterogeneity**

# A Brief History of the Field

Where are we now?

- Strong convergence of theory and empirics
- Wide range of topics under study from both theoretical and empirical perspectives (offshoring, multinationals, growth, innovation, trade policy, international institutions (GATT/WTO), political economy)
- Remarkable growth of new data sources (multi-origin sourcing of firms, multi-destination sales of firms, multi-product sourcing/sales of firms, household scanner data, better price data, firms, firms matched to matched firms, workers matched to firms, remote sensing, multinationals) often particularly rich in developing countries
- Heightened integration of intra-national and inter-national trade/spatial issues (e.g. richer notion of space; allowing for factor mobility)

# The Role of Empirics in International Trade

- There is a rich interaction between theory and empirics in International Trade that is perhaps without comparison in most areas of economics.
- The evolution of the theoretical study of trade since 1975 has been heavily influenced by empirical work. Some examples:
  - Evidence on intra-industry trade, trade between similar countries  $\Rightarrow$  'New trade theory' in 1980s (e.g. Krugman, 1980).
  - Evidence on within-industry heterogeneity, firm-level facts about exporters  $\Rightarrow$  firm-level approach to trade (e.g. Melitz, 2003).
  - More recent developments have been heavily data-driven: intra-firm trade, multinational production, multiproduct firms.
  - Ongoing debates about 'trade and wage inequality': continuous feedback of empirical findings into debate about sets of theories that are empirically relevant.

- We will see examples of wide range of empirical methods:
  - Descriptive methods and simple tests.
  - 'Reduced-form' econometric methods (ie not explicitly estimating model parameters): *Mostly Harmless Econometrics* is a great resource for learning these methods.
  - 'Structural' econometric methods: no textbook, but Reiss and Wolak (2007, *Handbook of Econometrics* chapter), Paarsch and Hong (2006, Auctions book) and Akerberg, Benkard, Berry and Pakes (2007, *Handbook of Econometrics* chapter) are great introductions.
  - 'Sufficient statistic' approaches (e.g. Chetty, ARE 2009).

# Is Empirical Trade Different?

(From empirical work in other fields...)

- Empirical work in trade is typically theory-driven, but not always explicitly 'structural':
  - But history of famous mistakes from empirical work not taking theory seriously enough have left their mark on the field.
  - Impossible to do empirical work without solid theoretical understanding.
- Unique tension:
  - Like macro: studying policy issues that are national in nature (e.g. tariffs).
  - Unlike macro: essential feature and focus is heterogeneity (across countries, industries, firms, factors, consumers, intra-national locations...)
- General equilibrium
  - *Interaction* between heterogeneous agents is paramount.
  - E.g., in basic  $2 \times 2$  Ricardian model, if you think in PE you conclude that absolute advantage matters, but if you think in GE you conclude that comparative advantage (ie interactions crucial).

# How Do You Do GE Empirics?

A common theme in this course

- Other heavily empirical fields are rarely forced to (or choose to) grapple with GE.
- But there are some great exceptions that include:
  - Labor: Heckman, Lochner and Taber (AERPP, 1998). Peer effects literature (e.g. Manski, Restud 1993). Acemoglu, Autor and Lyle (JPE 2004) on large labor supply shock. National-level (e.g. Borjas) vs city-level (e.g. Card) approach to immigration. Crepon et al (2012 QJE) on labor market policies.
  - Macro: Caballero-Engel (various), Bloom (Ecta 2007).
  - PF/Health: Finkelstein (QJE 2007) on individual-level vs aggregate (state)-level estimated effects of medicare.
  - Development: Miguel and Kremer (Ecta 2004) on de-worming spillovers across children within villages.
  - IO: Strategic interactions between firms within industries (Ericsson and Pakes (Restud, 1995); Bajari, Benkard and Levin (Ecta, 2007); Bajari, Hong and Nekipelov (2010) survey of game estimation literature; and many more).

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# International Trade: Standard Assumptions

- What distinguishes trade theory from abstract general-equilibrium analysis is the existence of a **hierarchical market structure**:
  - ① **“International”** good markets
  - ② **“Domestic”** factor markets
- Typical asymmetry between **“goods”** and **“factors”**:
  - Goods enter consumers' utility functions directly, are elastically supplied and demanded, and can be freely traded internationally
  - Factors only affect utility through the goods they generate, they are in fixed supply domestically, and they cannot be traded at all
- **Central Issues**:
  - How does the integration of good markets affect good prices?
  - How do changes in good prices, in turn, affect factor prices, factor allocation, production, and welfare?

# International Trade: Standard Assumptions (Cont.)

- While these assumptions are less fundamental, we will also often assume that:
  - Consumers have identical homothetic preferences in each country (representative agent)
  - Model is static (long-run view)
- Many of these assumptions look very strong, but they can be dealt with by clever reinterpretations of the model:
  - Transport costs could be handled by interpreting one of the good as transportation services
  - Factor mobility could be dealt with by defining as a good anything that can be traded
  - Goods and factors can be distinguished by locations, time, and states of nature

# Neoclassical Trade: Standard Assumptions

- **“Neoclassic trade models”** characterized by three key assumptions:
  - ① *Perfect competition*
  - ② *Constant returns to scale (CRS)*
  - ③ *No distortions*
  
- **Comments:**
  - We could allow for decreasing returns to scale (DRS) by introducing hidden factors in fixed supply
  - Increasing returns to scale (IRS) are a much more severe issue addressed by “New” trade theory (see lectures 8 and 9)

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# Neoclassical Trade: General Results

- Not surprisingly, there are few results that can be derived using only Assumptions 1-3
- In future lectures, we will derive sharp predictions for special cases: Ricardo, Assignment, Ricardo-Viner, and Heckscher-Ohlin models
- Today, we'll stick to the general case and show how simple revealed preference arguments can be used to establish two important results:
  - 1 *Gains from trade* (Samuelson 1939)
  - 2 *Law of comparative advantage* (Deardorff 1980)

- Consider a world economy with  $n = 1, \dots, N$  countries, each populated by  $h = 1, \dots, H_n$  households
- There are  $g = 1, \dots, G$  goods:
  - $y^n \equiv (y_1^n, \dots, y_G^n) \equiv$  Output vector in country  $n$
  - $c^{nh} \equiv (c_1^{nh}, \dots, c_G^{nh}) \equiv$  Consumption vector of household  $h$  in country  $n$
  - $p^n \equiv (p_1^n, \dots, p_G^n) \equiv$  Good price vector in country  $n$
- There are  $f = 1, \dots, F$  factors:
  - $v^n \equiv (v_1^n, \dots, v_F^n) \equiv$  Endowment vector in country  $n$
  - $w^n \equiv (w_1^n, \dots, w_F^n) \equiv$  Factor price vector in country  $n$

# Supply

## The revenue function

- We denote by  $\Omega^n$  the set of combinations  $(y, v)$  that are feasible in country  $n$ 
  - CRS  $\Rightarrow \Omega^n$  is a convex cone
- **Revenue function** in country  $n$  is defined as

$$r^n(p, v) \equiv \max_y \{py \mid (y, v) \in \Omega^n\}$$

- Comments (see Dixit-Norman pp. 31-36 for details):
  - Revenue function summarizes all relevant properties of technology
  - Under perfect competition,  $y^n$  maximizes the value of output in country  $n$ :

$$r^n(p^n, v^n) = p^n y^n \quad (1)$$

# Demand

## The expenditure function

- We denote by  $u^{nh}$  the utility function of household  $h$  in country  $n$
- **Expenditure function** for household  $h$  in country  $n$  is defined as

$$e^{nh}(p, u) = \min_c \{ pc \mid u^{nh}(c) \geq u \}$$

- Comments (see Dixit-Norman pp. 59-64 for details):
  - Here factor endowments are in fixed supply, but easy to generalize to case where households choose factor supply optimally
  - Holding  $p$  fixed,  $e^{nh}(p, u)$  is increasing in  $u$
  - Household's optimization implies

$$e^{nh}(p^n, u^{nh}) = p^n c^{nh}, \quad (2)$$

where  $c^{nh}$  and  $u^{nh}$  are the consumption and utility level of the household in equilibrium, respectively

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# Gains from Trade

One household per country

- In the next propositions, when we say “*in a neoclassical trade model,*” we mean in a model where equations (1) and (2) hold in any equilibrium.
- Consider first the case where there is just one household per country
- Without risk of confusion, we drop  $h$  and  $n$  from all variables
- Instead we denote by:
  - $(y^a, c^a, p^a)$  the vector of output, consumption, and good prices under autarky
  - $(y, c, p)$  the vector of output, consumption, and good prices under free trade
  - $u^a$  and  $u$  the utility levels under autarky and free trade

# Gains from Trade

One household per country

- **Proposition 1** *In a neoclassical trade model with one household per country, free trade makes all households in the world (weakly) better off.*
- Proof:

$$\begin{aligned} e(p, u^a) &\leq pc^a, && \text{by definition of } e(\cdot) \\ &= py^a && \text{by market clearing under autarky} \\ &\leq r(p, v) && \text{by definition of } r(\cdot) \\ &= e(p, u) && \text{by equations (1), (2), and trade balance} \end{aligned}$$

Since  $e(p, \cdot)$  increasing, we get  $u \geq u^a$

# Gains from Trade

One household per country

- **Comments:**

- Two inequalities in the previous proof correspond to consumption and production gains from trade
- Previous inequalities are weak. Equality if kinks in IC or PPF
- Previous proposition only establishes that households always prefer “free trade” to “autarky.” It does **not** say anything about the comparisons of trade equilibria

# Gains from Trade

Multiple households per country (I): domestic lump-sum transfers

- With multiple-households, moving away from autarky is likely to create winners and losers
- In order to establish the Pareto-superiority of trade, we will therefore need to allow for policy instruments. We start with *domestic* lump-sum transfers and then consider commodity/factor-based taxes.
- We now reintroduce the index  $h$  explicitly and denote by:
  - $c^{ah}$  and  $c^h$  the vector of consumption of household  $h$  under autarky and free trade
  - $v^{ah}$  and  $v^h$  the vector of endowments of household  $h$  under autarky and free trade
  - $u^{ah}$  and  $u^h$  the utility levels of household  $h$  under autarky and free trade
  - $\tau^h$  the lump-sum transfer from the government to household  $h$  ( $\tau^h \leq 0 \Leftrightarrow$  lump-sum tax and  $\tau^h \geq 0 \Leftrightarrow$  lump-sum subsidy)

# Gains from Trade

Multiple households per country (I): domestic lump-sum transfers

- **Proposition 2** *In a neoclassical trade model with multiple households per country, there exist domestic lump-sum transfers such that free trade is (weakly) Pareto superior to autarky in all countries*
- **Proof:** We proceed in two steps...

Step 1: For any  $h$ , set the lump-sum transfer  $\tau^h$  such that

$$\tau^h = (p - p^a) c^{ah} - (w - w^a) v^h$$

Budget constraint under autarky implies  $p^a c^{ah} \leq w^a v^h$ . Therefore

$$p c^{ah} \leq w v^h + \tau^h$$

Thus  $c^{ah}$  is still in the budget set of household  $h$  under free trade

# Gains from Trade

Multiple households per country (I): domestic lump-sum transfers

- **Proposition 2** *In a neoclassical trade model with multiple households per country, there exist domestic lump-sum transfers such that free trade is (weakly) Pareto superior to autarky in all countries*

- **Proof (Cont.):**

Step 2: By definition, government's revenue is given by

$$\begin{aligned} -\sum \tau^h &= (p^a - p) \sum c^{ah} - (w^a - w) \sum v^h && : \text{definition of } \tau_h \\ &= (p^a - p) y^a - (w^a - w) v && : \text{mc autarky} \\ &= -py^a + wv && : \text{zp autarky} \\ &\geq -r(p, v) + wv && : \text{definition } r(p, v) \\ &= -(py - wv) = 0 && : \text{eq. (1) + zp free trade} \end{aligned}$$

# Gains from Trade

Multiple households per country (I): domestic lump-sum transfers

- **Comments:**

- Good to know we don't need *international* lump-sum transfers
- But these domestic lump-sum transfers remain informationally intensive ( $c^{ah?}$ )

# Gains from Trade

Multiple households per country (II): commodity and factor taxation

- With this last comment in mind, we now restrict the set of instruments to commodity and factor taxes/subsidies
- More specifically, suppose that the government can affect the prices faced by all households under free trade by setting  $\tau^{\text{good}}$  and  $\tau^{\text{factor}}$

$$\begin{aligned} p^{\text{household}} &= p + \tau^{\text{good}} \\ w^{\text{household}} &= w + \tau^{\text{factor}} \end{aligned}$$

# Gains from Trade

Multiple households per country (II): commodity and factor taxation

- **Proposition 3** *In a neoclassical trade model with multiple households per country, there exist commodity and factor taxes/subsidies such that free trade is (weakly) Pareto superior to autarky in all countries*
- **Proof:** Consider the two following taxes:

$$\begin{aligned}\tau^{\text{good}} &= p^a - p \\ \tau^{\text{factor}} &= w^a - w\end{aligned}$$

By construction, household is indifferent between autarky and free trade. Now consider government's revenues. By definition

$$\begin{aligned}-\sum \tau^h &= \tau^{\text{good}} \sum c^{ah} - \tau^{\text{factor}} \sum v^h \\ &= (p^a - p) \sum c^{ah} - (w^a - w) \sum v^h \geq 0,\end{aligned}$$

for the same reason as in the previous proof.

# Gains from Trade

Multiple households per country (II): commodity and factor taxation

- **Comments:**

- Previous argument only relies on the existence of *production gains* from trade
- If there is a kink in the PPF, we know that there aren't any...
- Factor taxation still informationally intensive: need to know endowments in efficiency units, may lead to different taxes across firms

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# Law of Comparative Advantage

## Basic Idea

- The previous results have focused on normative predictions
- We now demonstrate how the same revealed preference argument can be used to make positive predictions about the pattern of trade
- **Principle of comparative advantage:**  
Comparative advantage—meaning differences in relative autarky prices—is the basis for trade
- Why? If two countries have the same autarky prices, then after opening up to trade, the autarky prices remain equilibrium prices. So there will be no trade....
- **The law of comparative advantage (in words):**  
Countries tend to export goods in which they have a CA, i.e. lower relative autarky prices compared to other countries

# Law of Comparative Advantage

Dixit and Norman (1980), Deardorff (1980)

- Let  $t^n \equiv (y_1^n - \sum c^{nh}, \dots, y_G^n - \sum c^{nh})$  denote net exports in country  $n$
- Let  $u^{an}$  and  $u^n$  denote the utility level of the representative household in country  $n$  under autarky and free trade
- Let  $p^{an}$  denote the vector of autarky prices in country  $n$
- Without loss of generality, normalize prices such that:

$$\sum p_g = \sum p_g^{an} = 1,$$

- Notation:

$$\begin{aligned} \text{cor}(x, y) &= \frac{\text{cov}(x, y)}{\sqrt{\text{var}(x) \text{var}(y)}} \\ \text{cov}(x, y) &= \sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y}) \\ \bar{x} &= \frac{1}{n} \sum_{i=1}^n x_i \end{aligned}$$

# Law of Comparative Advantage

Dixit and Norman (1980), Deardorff (1980)

- **Proposition 4** *In a neoclassical trade model, if there is a representative household in country  $n$ , then  $\text{cor}(p - p^a, t^n) \geq 0$*

**Proof:** Since  $(y^n, v^n) \in \Omega^n$ , the definition of  $r$  implies

$$p^a y^n \leq r(p^a, v^n)$$

Since  $u^n(c^n) = u^n$ , the definition of  $e$  implies

$$p^a c^n \geq e(p^a, u^n)$$

The two previous inequalities imply

$$p^a t^n \leq r(p^a, v^n) - e(p^a, u^n) \quad (3)$$

Since  $u^n \geq u^{an}$  by Proposition 1,  $e(p^a, \cdot)$  increasing implies

$$e(p^a, u^n) \geq e(p^a, u^{na}) \quad (4)$$

# Law of Comparative Advantage

Dixit and Norman (1980), Deardorff (1980)

- **Proposition 4** *In a neoclassical trade model, if there is a representative household in country  $n$ , then  $\text{cor}(p - p^a, t^n) \geq 0$*   
**Proof (Cont.):** Combining inequalities (3) and (4), we obtain

$$p^a t^n \leq r(p^a, v^n) - e(p^a, u^{na}) = 0,$$

where the equality comes from market clearing under autarky. Because of balanced trade, we know that

$$p t^n = 0$$

Hence

$$(p - p^a) t^n \geq 0$$

# Law of Comparative Advantage

Dixit and Norman (1980), Deardorff (1980)

- **Proposition 4** *In a neoclassical trade model, if there is a representative household in country  $n$ , then  $\text{cor}(p - p^a, t^n) \geq 0$*

**Proof (Cont.):** By definition,

$$\text{cov}(p - p^a, t^n) = \sum_g (p_g - p_g^a - \bar{p} + \bar{p}^a) (t_g^n - \bar{t}^n),$$

which can be rearranged as

$$\text{cov}(p - p^a, t^n) = (p - p^a) t^n + G (\bar{p} - \bar{p}^a) \bar{t}^n$$

Given our price normalization, we know that  $\bar{p} = \bar{p}^a$ . Hence

$$\text{cov}(p - p^a, t^n) = (p - p^a) t^n \geq 0$$

Proposition 4 derives from this observation and the fact that

$$\text{sign}[\text{cor}(p - p^a, t^n)] = \text{sign}[\text{cov}(p - p^a, t^n)]$$

# Law of Comparative Advantage

Dixit and Norman (1980), Deardorff (1980)

## • Comments:

- With 2 goods, each country exports the good in which it has a CA, but with more goods, this is just a correlation
- Core of the proof is the observation that  $p^a t^n \leq 0$
- It directly derives from the fact that there are gains from trade. Since free trade is better than autarky, the vector of consumptions must be at most barely attainable under autarky ( $p^a y^n \leq p^a c^n$ )
- For empirical purposes, problem is that we rarely observe autarky...(but see next lecture for a nice example).
- In future lectures, we will look at models which relate  $p^a$  to (observable) primitives of the model (technology and factor endowments) in order to make progress.